

### **Today's Menu**

- Introduction to machine learning
  - Unsupervised, supervised and reinforcement learning
- Clustering
  - K-means clustering
- Hierarchical clustering
- Heatmap representations
- Dimensionality reduction, visualization and 'structure' analysis
  - Principal Component Analysis (PCA)
- Hands-on application to cell classification

### Types of machine learning

- <u>Unsupervised learning</u>
  - Finding structure in unlabeled data
- Supervised learning
  - Making predictions based on labeled data
  - Predictions like regression or classification
- <u>Reinforcement learning</u>
  - Making decisions based on past experience

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- You define *k* the number of clusters!

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Here your eyes can clearly see 3 natural groupings

#### k-means clustering algorithm

- Breaks observations into *k* pre-defined number of clusters
- You define *k* the number of clusters!
  - Imagine you had data that you could plot along a line and you knew you had to put them into k=3 "clusters" (e.g. data from three types of tumor cells)

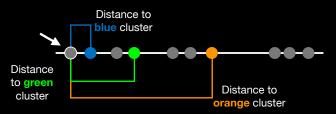


Here your eyes can clearly see 3 natural groupings How does k-means attempt to define this grouping? Step 1. Select *k* (the number of clusters)



#### Step 3.

Measure distance between the 1st point and the **k=3** initial clusters



Step 2. Select *k=3* distant data points at random These are the initial clusters

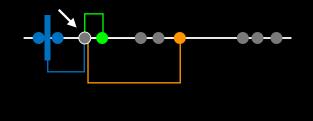


Step 4. Assign the 1st point to the nearest cluster

#### Step 6.

Assign next point to closest cluster

Use updated cluster centers for distance calculation



#### Step 5.

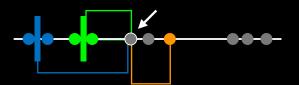
#### Update cluster centers

Calculate the mean value for the blue cluster including the new point



#### Step 7.

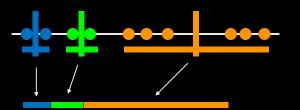
Update cluster centers and move to next point Use updated cluster centers for distance calculation



Step 8. Repeat for each point Each time updating cluster centers



Assess the quality of the clustering by adding up the variation within each cluster

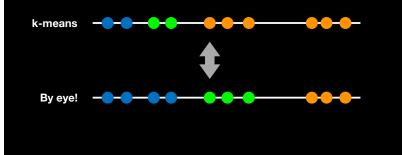


The total variation within clusters

K-means keeps track of these clusters and their total **variance** and then does the whole thing over again with different starting points

#### Hmm....

Here the k-means result does not look as good as what we were able to do by eye!



#### Step 10.

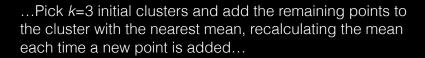
Repeat with different starting points Back to the beginning and do all steps over again...





Pick new points as "initial" clusters

...Pick k=3 initial clusters and add the remaining points to the cluster with the nearest mean, recalculating the mean each time a new point is added...





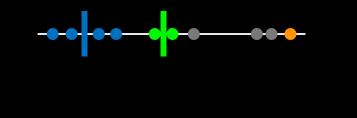
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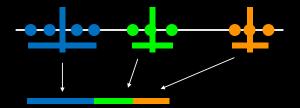
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Now the data are all assigned to clusters, we again sum the variation within each cluster



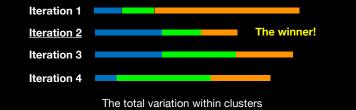
The total variation within clusters

Step 10. Repeat again with different starting points

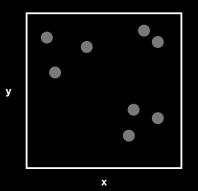


After several iterations k-means clustering knows it has the <u>best clustering so-far</u> based on the smallest total variation with clusters.

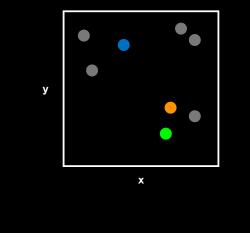
However, it does not know if it has found the *best overall*. So it will perform several more iterations with different starting points...



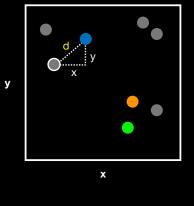
# What if we have more dimensions?



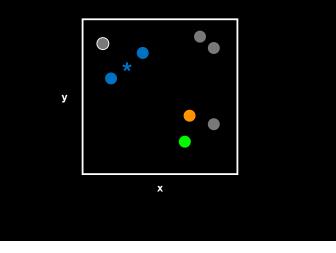
Just like before, we pick 3 random points...



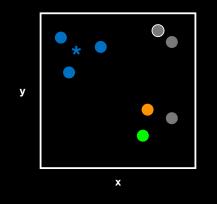
...and use the Euclidean distance. In 2 dimensions the Euclidean distance is the same as the Pythagorean theorem  $d = sqrt(x^2 + y^2)$ 

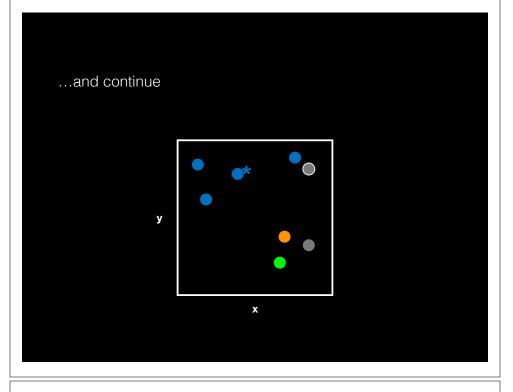


...assign point to nearest cluster and update cluster center \*

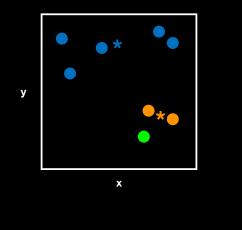


...and continue

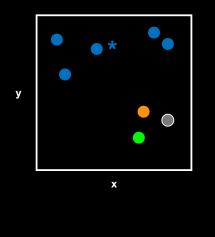




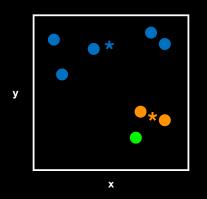
#### ...and continue



#### ...and continue



# Again we have to use a number of different starting conditions before deciding on a good clustering!



# What if we have even more dimensions?

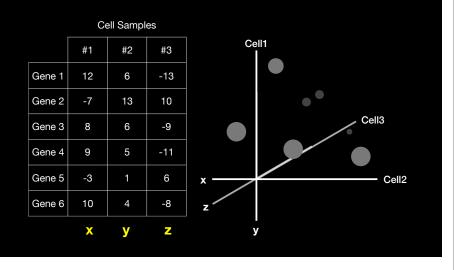
	Cell Samples				
	#1	#2	#3		
Gene 1	12	6	-13		
Gene 2	-7	13	10		
Gene 3	8	6	-9		
Gene 4	9	5	-11		
Gene 5	-3	1	6		
Gene 6	10	4	-8		

# What if we have even more dimensions?

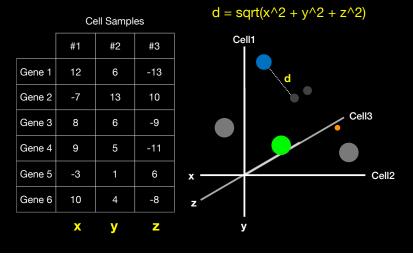
	X	У	z		
Gene 6	10	4	-8		
Gene 5	-3	1	6		
Gene 4	9	5	-11		
Gene 3	8	6	-9		
Gene 2	-7	13	10		
Gene 1	12	6	-13		
	#1	#2	#3		
	Cell Samples				

We could simply plot them by relabeling the cell samples as **x**, **y**, and **z** (i.e. a 3D plot)

# What if we have even more dimensions?



...and go through exactly the same procedure with initial cluster assignment followed by distance calculation etc...



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	Cell Samples					
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Gene 5	-3	1	6			
Gene 6	10	4	-8			

 $d = sqrt(x^2 + y^2 + z^2)$ 

Of course we don't actually need to plot anything.

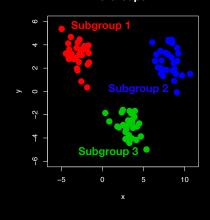
We can just calculate the Euclidean distance along any number of dimensions and perform our k-means clustering in the same way.

# k-means in R

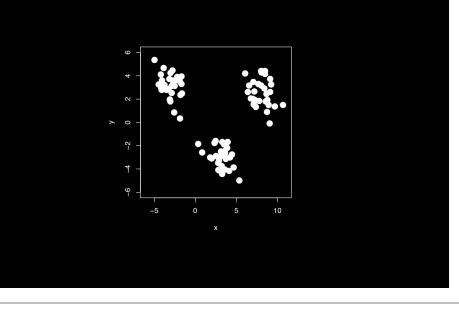
# k-means algorithm with 3 centers, run 20 times
kmeans(x, centers= 3, nstart= 20)

- Input x is a numeric matrix, or data.frame, with one observation per row, one feature per column
- k-means has a random component
- Run algorithm multiple times to improve odds of the best model

# Run k-means algorithm with 3 centers, run 20 times
kmeans(x, centers=3, nstart=20)



#### 3 Groups



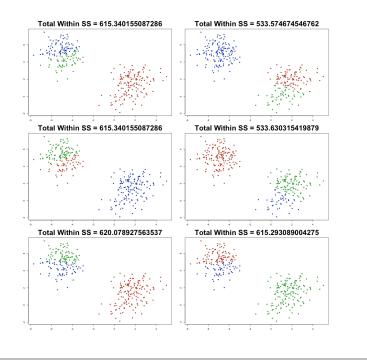
### Model selection

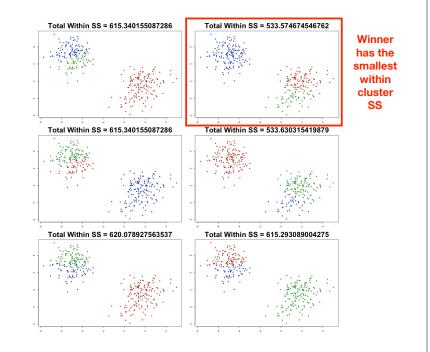
- · Recall k-means has a random component
- Best outcome is based on total within cluster sum of squares:
  - For each cluster
    - For each observation in the cluster
      - Determine squared distance from observation to cluster center
  - Sum all of them together

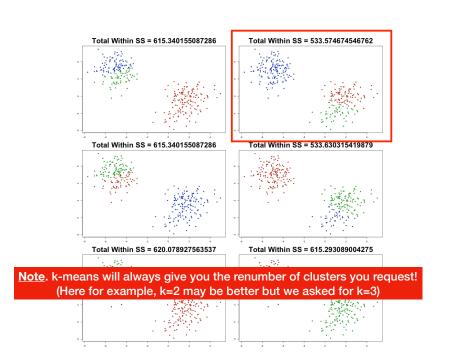
# Model selection

# k-means algorithm with 5 centers, run 20 times
kmeans(x, centers=5, nstart=20)

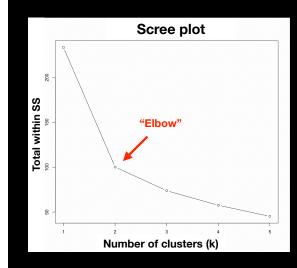
- Running algorithm multiple times (i.e. setting nstart) helps find the global minimum total within cluster sum of squares
- Increasing the default value of **nstart** is often sensible







#### Determining number of clusters



Trial and error is not the best approach

Systematically try a range of different k values and plot a "scree plot".

Here there is a large reduction in SS with **k=2** but after that the values do not go down as quickly!

#### Your Turn!

# Generate some example data for clusterin
tmp <- c(rnorm(30,-3), rnorm(30,3))
x <- cbind(x=tmp, y=rev(tmp))</pre>

#### plot(x)

Use the kmeans() function setting k to 2 and nstart=20

Inspect/print the results

- Q. How many points are in each cluster?
- Q. What 'component' of your result object details
  - cluster size?
  - cluster assignment/membership?
  - cluster center?

Plot x colored by the kmeans cluster assignment and add cluster centers as blue points

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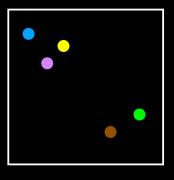
### Hierarchical clustering

- Number of clusters is not known ahead of time
- Two kinds of hierarchical clustering:
  - bottom-up
  - top-down

## Hierarchical clustering

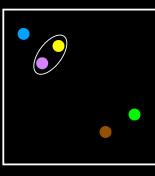
Simple example:

5 clusters: Each point starts as it's own "cluster"!



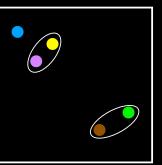
### Hierarchical clustering

4 clusters



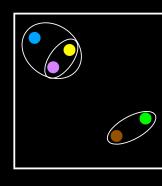
# Hierarchical clustering

3 clusters



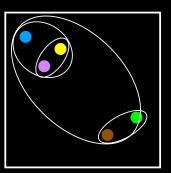
### Hierarchical clustering

2 clusters



### Hierarchical clustering

End: 1 cluster



#### Hierarchical clustering in R

# First we need to calculate point (dis)similarity
# as the Euclidean distance between observations
dist\_matrix <- dist(x)</pre>

/ The helust() function returns a hierarchical
/ clustering model
he <- helust(d = dist\_matrix)</pre>

che peint method is not so useful here
hc
Call:
hclust(d = dist\_matrix)

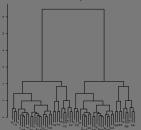
Cluster method : complete Distance : euclidean Number of objects: 60

# Interpreting results

# Create hierarchical cluster model: ho
hc <- hclust(dist(x))</pre>

# We can plot the results as a dendsogram
plot(hc)

# What do you notice?
# Does the dendrogram
# make sense based on
# your knoweledge of x?



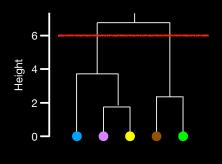
# Dendrogram Dendrogram • Tree shaped structure used to interpret • Tree shaped structure used to interpret hierarchical clustering models hierarchical clustering models Height Heighl Dendrogram Dendrogram • Tree shaped structure used to interpret • Tree shaped structure used to interpret hierarchical clustering models hierarchical clustering models Height Height

# Dendrogram Dendrogram • Tree shaped structure used to interpret • Tree shaped structure used to interpret hierarchical clustering models hierarchical clustering models Height Height Dendrogram plotting in R

plot(hc) 6. Height 2-0 -

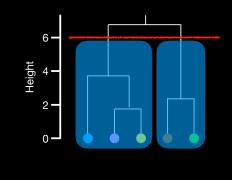
# Dendrogram plotting in R

plot(hc) abline(h=6, col="red")



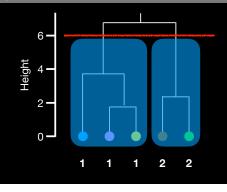
### Dendrogram plotting in R

# Draws a dendrogram
plot(hc)
abline(h=6, col="red")



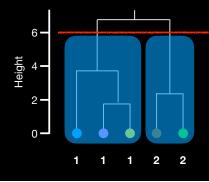
# Dendrogram plotting in R

# Draws a dendrogram
plot(hc)
abline(h=6, col="red")
cutree(hc, h=6) # Cut by height
[1] 1,1,1,2,2



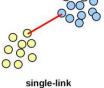
# Dendrogram plotting in R

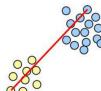
# Draws a dendrogram
plot(hc)
abline(h=6, col="red")
cutree(hc, k=2 ) # Cut into k grps
[1] 1,1,1,2,2



# Linking clusters in hierarchical clustering

- How is distance between clusters determined?
- There are four main methods to determine which cluster should be linked:
  - Complete: pairwise similarity between all observations in cluster 1 and cluster 2, and uses largest of similarities
  - Single: same as above but uses smallest of similarities
  - Average: same as above but uses average of similarities
  - Centroid: finds centroid of cluster 1 and centroid of cluster 2, and uses similarity between two centroids

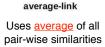




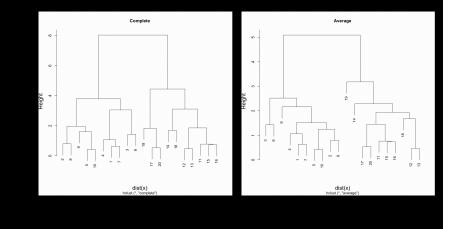


Uses smallest of all pair-wise similarities

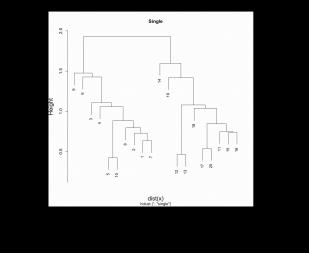
complete-link Uses largest of all pair-wise similarities



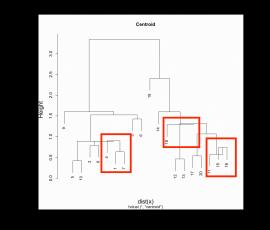
#### Linking methods: complete and average



# Linking method: single



# Linking method: centroid



## Linkage in R

# Using different hierarchical clustering method hc.complete <- hclust(d, method="complete")</pre>

hc.average <- hclust(d, method="average")</pre>

hc.single <- hclust(d, method="single")</pre>

#### Your Turn!

plot(x, col=col)

Q. Use the dist(), hclust(), plot() and cutree()
 functions to return 2 and 3 clusters
Q. How does this compare to your known 'col' groups?

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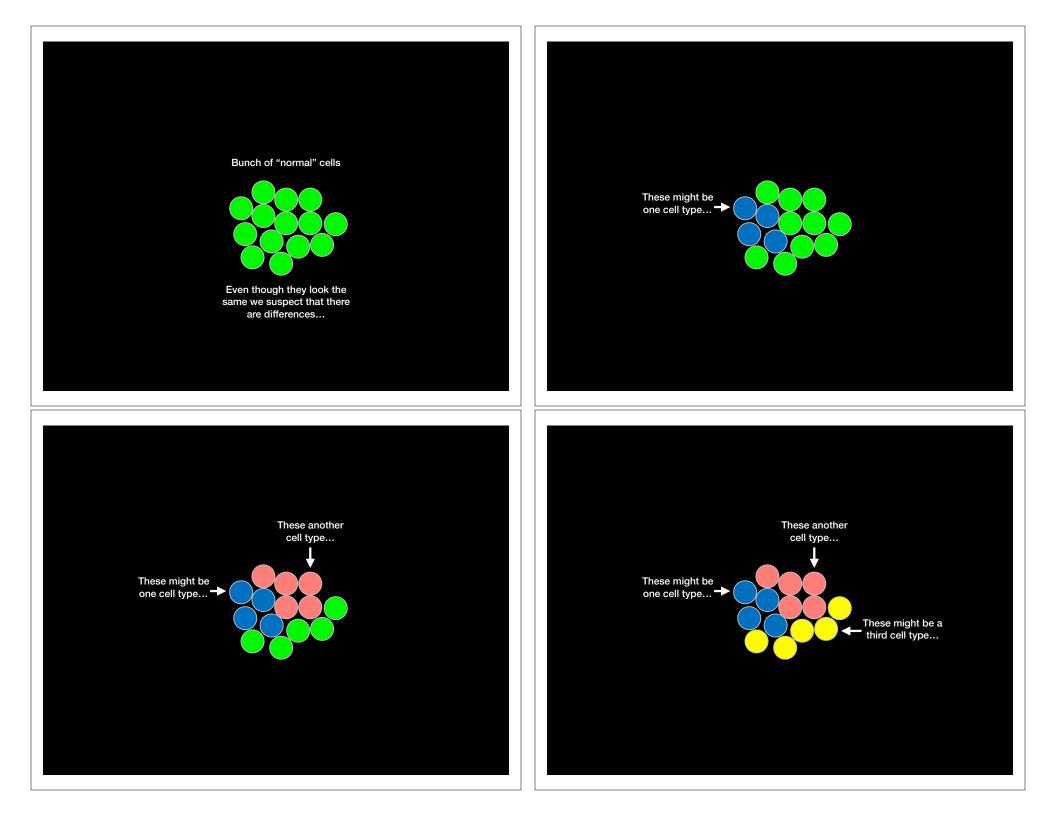
• Principal Component Analysis (PCA)

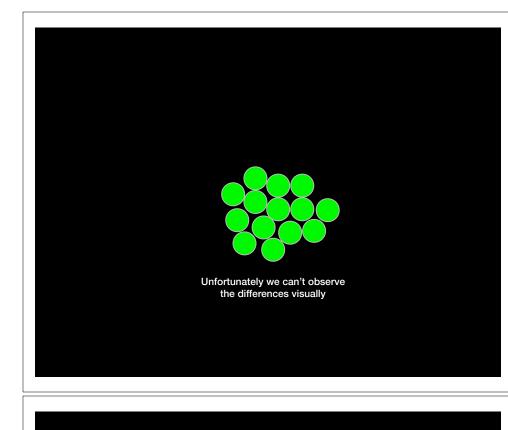
• Hands-on application to cell classification

#### **PCA: The absolute basics**

#### Bunch of "normal" cells









Unfortunately we can't observe the differences visually

So we sequence the mRNA in each cell to identify which genes are active and at what levels.

#### Each column shows how much each gene is transcribed in each cell

	Cell1	Cell2	Cell3	Cell4	
Gene1	3	0.25	2.8	0.1	
Gene2	2.9	0.8	2.2	1.8	
Gene3	2.2	1	1.5	3.2	
Gene4	2	1.4	2	0.3	
Gene5	1.3	1.6	1.6	0	
Gene6	1.5	2	2.1	3	
Gene7	1.1	2.2	1.2	2.8	
Gene8	1	2.7	0.9	0.3	
Gene9	0.4	3	0.6	0.1	

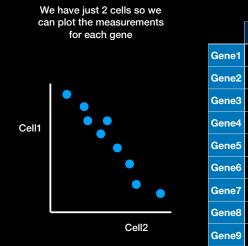
Here is the data...

_					
Gene1	3	0.25	2.8	0.1	
Gene2	2.9	0.8	2.2	1.8	
Gene3	2.2	1	1.5	3.2	
Gene4	2	1.4	2	0.3	
Gene5	1.3	1.6	1.6	0	
Gene6	1.5	2	2.1	3	
Gene7	1.1	2.2	1.2	2.8	
Gene8	1	2.7	0.9	0.3	
Gene9	0.4	3	0.6	0.1	

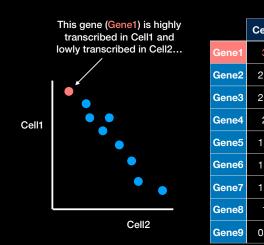
Cell1 Cell2 Cell3 Cell4

Here is the data...

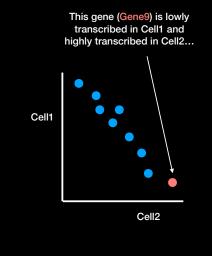
		Cell1	Cell2
		Cent	Cellz
	Gene1	3	0.25
	Gene2	2.9	0.8
	Gene3	2.2	1
For now lets consider only two cells	Gene4	2	1.4
	Gene5	1.3	1.6
	Gene6	1.5	2
	Gene7	1.1	2.2
	Gene8	1	2.7
	Gene9	0.4	3



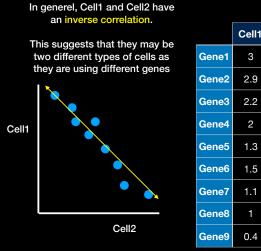
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Gene7	1.1	2.2
Gene8	1	2.7
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Gene5	1.3	1.6
Gene6	1.5	2
Gene7	1.1	2.2
Gene8	1	2.7
Gene9	0.4	3

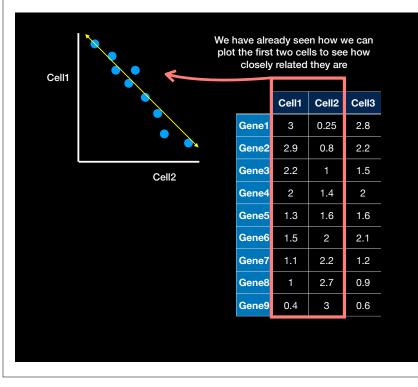


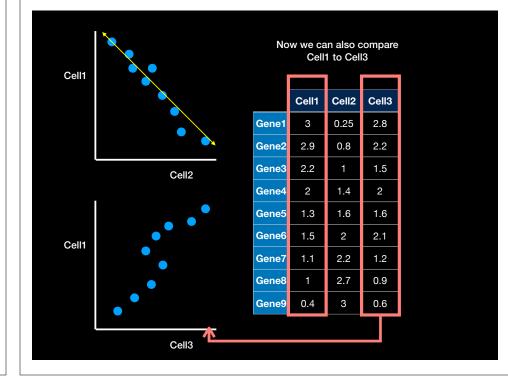
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Gene4	2	1.4
Gene5	1.3	1.6
Gene6	1.5	2
Gene7	1.1	2.2
Gene8	1	2.7
Gene9	0.4	3

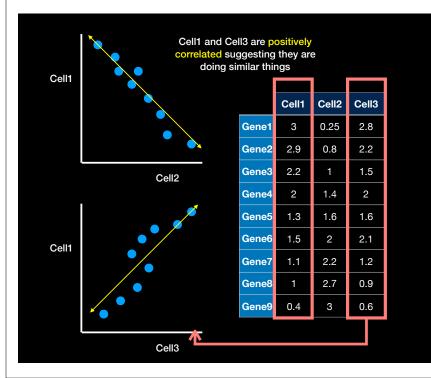


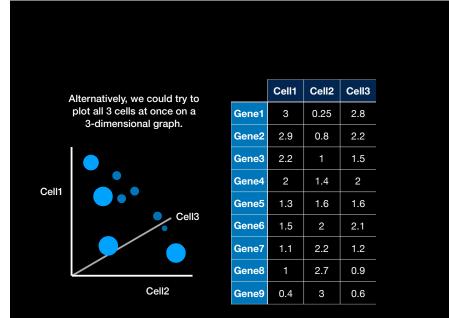
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Gene6	1.5	2
Gene7	1.1	2.2
Gene8	1	2.7
Gene9	0.4	3

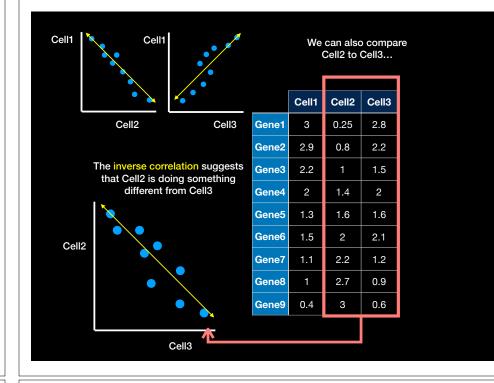
		Cell1	Cell2	Cell3
	Gene1	3	0.25	2.8
	Gene2	2.9	0.8	2.2
	Gene3	2.2	1	1.5
Now lets imagine there are three cells	Gene4	2	1.4	2
	Gene5	1.3	1.6	1.6
	Gene6	1.5	2	2.1
	Gene7	1.1	2.2	1.2
	Gene8	1	2.7	0.9
	Gene9	0.4	3	0.6





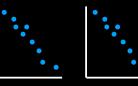




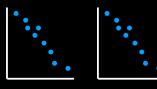


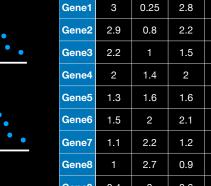
#### But what if we have 4 or more Cells?

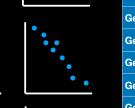
	Cell1	Cell2	Cell3	Cell4	
Gene1	3	0.25	2.8	0.1	
Gene2	2.9	0.8	2.2	1.8	
Gene3	2.2	1	1.5	3.2	
Gene4	2	1.4	2	0.3	
Gene5	1.3	1.6	1.6	0	
Gene6	1.5	2	2.1	3	
Gene7	1.1	2.2	1.2	2.8	
Gene8	1	2.7	0.9	0.3	
Gene9	0.4	3	0.6	0.1	

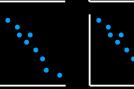


#### Draw lots of 2 cell plots and try to make sense of them all?





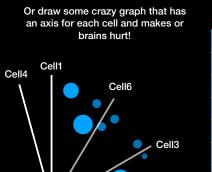




Gene2	2.9	0.8	2.2	1.8	
Gene3	2.2	1	1.5	3.2	
Gene4	2	1.4	2	0.3	
Gene5	1.3	1.6	1.6	0	
Gene6	1.5	2	2.1	3	
Gene7	1.1	2.2	1.2	2.8	
Gene8	1	2.7	0.9	0.3	
Gene9	0.4	3	0.6	0.1	

Cell1 Cell2 Cell3 Cell4

0.1



Cell2

Cell6

	Cell1	Cell2	Cell3	Cell4	
Gene1	3	0.25	2.8	0.1	
Gene2	2.9	0.8	2.2	1.8	
Gene3	2.2	1	1.5	3.2	
Gene4	2	1.4 2		0.3	
Gene5	1.3	1.6 1.6		0	
Gene6	1.5	2	2.1	3	
Gene7	1.1	2.2	1.2	2.8	
Gene8	1	2.7	0.9	0.3	
Gene9	0.4	3	0.6	0.1	

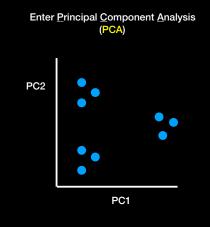


Cell6

Cell1

Cell4

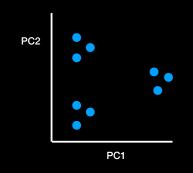
		Cell1	Cell2	Cell3	Cell4	
	Gene1	3	0.25	2.8	0.1	
	Gene2	2.9	0.8	2.2	1.8	
	Gene3	2.2	1	1.5	3.2	
	Gene4	2	1.4	2	0.3	
	Gene5	1.3	1.6	1.6	0	
ell3	Gene6	1.5	2	2.1	3	
	Gene7	1.1	2.2	1.2	2.8	
- Cell2	Gene8	1	2.7	0.9	0.3	
	Gene9	0.4	3	0.6	0.1	
-110						



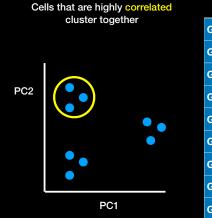
	Cell1	Cell2	Cell3	Cell4	
Gene1	3	0.25	2.8	0.1	
Gene2	2.9	0.8	2.2	1.8	
Gene3	2.2	1	1.5	3.2	
Gene4	2	2 1.4 2		0.3	
Gene5	1.3	1.6	1.6	0	
Gene6	1.5	2	2.1	3	
Gene7	1.1	2.2	1.2	2.8	
Gene8	1	2.7	0.9	0.3	
Gene9	0.4	3	0.6	0.1	

Cell6

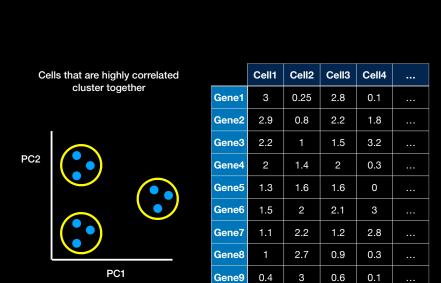
PCA converts the correlations (or lack there of) among all cells into a representation we can more readily interpret (e.g. a 2D graph!)

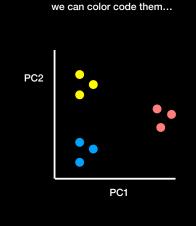


	Cell1	Cell2	Cell3	Cell4	
Gene1	3	0.25	2.8	0.1	
Gene2	2.9	0.8	2.2	1.8	
Gene3	2.2	1	1.5	3.2	
Gene4	2	1.4	2	0.3	
Gene5	1.3	1.6	1.6	0	
Gene6	1.5	2	2.1	3	
Gene7	1.1	2.2	1.2	2.8	
Gene8	1	2.7	0.9	0.3	
Gene9	0.4	3	0.6	0.1	



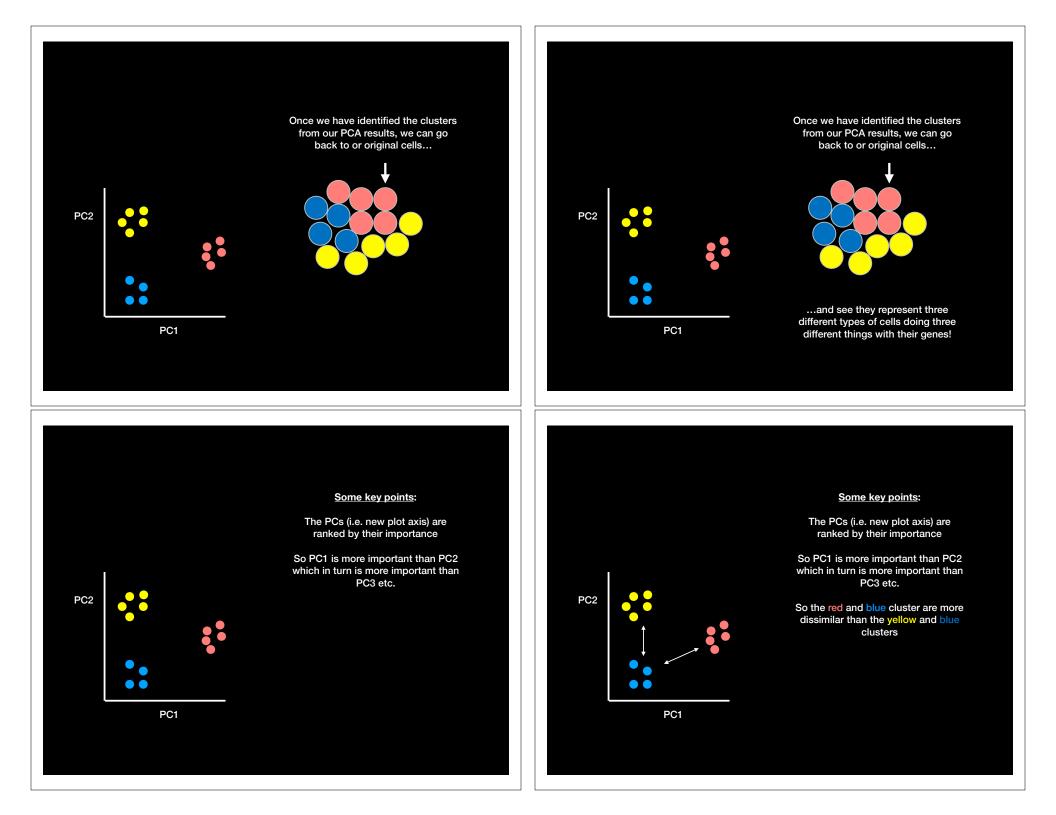
	Cell1	Cell2	Cell3	Cell4	
Gene1	3	0.25	2.8	0.1	
Gene2	2.9	0.8	2.2	1.8	
Gene3	2.2	1	1.5	3.2	
Gene4	2	1.4	2	0.3	
Gene5	1.3	1.6	1.6	0	
Gene6	1.5	2	2.1	3	
Gene7	1.1	2.2	1.2	2.8	
Gene8	1	2.7	0.9	0.3	
Gene9	0.4	3	0.6	0.1	

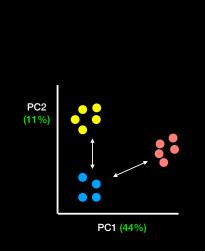




To make the clusters easier to see

	Cell1	Cell2	Cell3	Cell4	
Gene1	3	0.25	2.8	0.1	
Gene2	2.9	0.8	2.2	1.8	
Gene3	2.2	1	1.5	3.2	
Gene4	2	1.4	2	0.3	
Gene5	1.3	1.6	1.6	0	
Gene6	1.5	2	2.1	3	
Gene7	1.1	2.2	1.2	2.8	
Gene8	1	2.7	0.9	0.3	
Gene9	0.4	3	0.6	0.1	





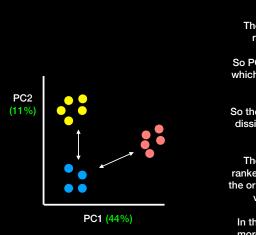
#### Some key points:

The PCs (i.e. new plot axis) are ranked by their importance

So PC1 is more important than PC2 which in turn is more important than PC3 etc.

So the red and blue cluster are more dissimilar than the yellow and blue clusters

The PCs (i.e. new plot axis) are ranked by the amount of variance in the original data (i.e. gene expression values) that they "capture"



gene64

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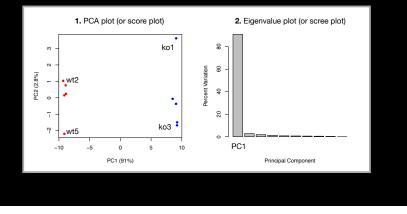
So the red and blue cluster are more dissimilar than the yellow and blue clusters

The PCs (i.e. new plot axis) are ranked by the amount of variance in the original data (i.e. gene expression values) that they "capture"

In this example PC1 'captures' 4xmore of the original variance than PC2 (44/11 = 4)

-0.1047629 -0.1047443

- · We actually get two main things out of a typical PCA
  - The new axis (called PCs or Eigenvectors) and
  - Eigenvalues that detail the amount of variance captured by each PC



#### **Bonus: PC Loadings**

- Another cool thing we can get out of PCA is a quantitive report on how the original variables contributed to each PC
  - In other words, which were the most important genes that lead to the observed clustering in PC-space
  - These are often called the loadings and we can plot them to see which are the most important genes for the observed separation as well as outputting ranked lists of genes that act to discriminate the samples

### Hands-on time!

https://bioboot.github.io/bggn213 W20/class-material/pca/

#### **Outline:** How to do PCA in R

- How to use the **prcomp()** function to do PCA.
- How to draw and interpret PCA plots
- How to determine how much variation each principal component accounts for and the the "intrinsic dimensionality" useful for further analysis
- How to examine the **loadings** (or loading scores) to determine what variables have the largest effect on the graph and are thus important for discriminating samples.

• First lets read our example data to work with.

##	You	can	also	download	this	file	from	the	class	website!
myc	data	<-	read.	<mark>csv</mark> ("http:	s://t	inyurl	L.com,	/exp:	ression	n-CSV",
				row.na	ames=1	L)				

head(mydata)

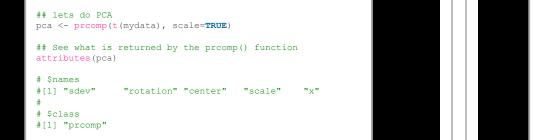
	wt1	wt2	wt3	wt4	wt5	ko1	ko2	ko3	ko4	ko5
gene1	147	171	160	175	187	63	57	58	55	59
gene2	151	134	148	126	134	838	831	894	847	830
gene3	702	672	653	681	701	593	579	644	596	610
gene4	319	297	310	296	304	754	807	734	750	774
gene5	168	147	162	142	152	787	811	814	869	784

• NOTE: the samples are columns, and the genes are rows!

- Now we have our data we call prcomp() to do PCA
  - NOTE: prcomp() expects the samples to be rows and genes to be columns so we need to first transpose the matrix with the t() function!

## lets do PCA
pca <- prcomp(t(mydata), scale=TRUE)</pre>

- Now we have our data we call **prcomp()** to do PCA
  - NOTE: prcomp() expects the samples to be rows and genes to be columns so we need to first transpose the matrix with the t() function!



- The returned pca\$x here contains the principal components (PCs) for drawing our first graph.
  - Here we will take the first two columns in pca\$x (corresponding to PC1 and PC2) to draw a 2-D plot

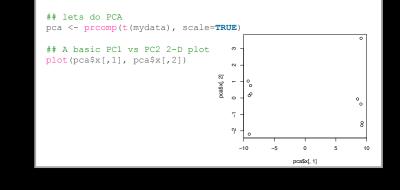
<pre>## lets do PCA pca &lt;- prcomp(t(mydata), scale=TRUE)</pre>	
<pre>## See what is returned by the prcomp() function attributes(pca)</pre>	
<pre># \$names #[1] "sdev" "rotation" "center" "scale" "x" # # \$class #[1] "prcomp"</pre>	

- The returned pca\$x here contains the principal components (PCs) for drawing our first graph.
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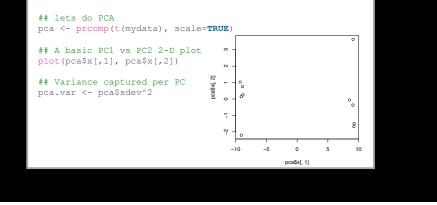
## lets do PCA
pca <- prcomp(t(mydata), scale=TRUE)</pre>

## A basic PC1 vs PC2 2-D plot
plot(pca\$x[,1], pca\$x[,2])

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- Looks interesting with a nice separation of samples into two groups of 5 samples each
  - Now we can use the square of pca\$sdev , which stands for "standard deviation", to calculate how much variation in the original data each PC accounts for



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plot(pca\$x[,1], pca\$x[,2])

## Precent variance is often more informative to look at
pca.var <- pca\$sdev^2
pca.var.per <- round(pca.var/sum(pca.var)\*100, 1)</pre>

pca.var.per

[1] 91.0 2.8 1.9 1.3 0.8 0.7 0.6 0.5 0.3 0.0

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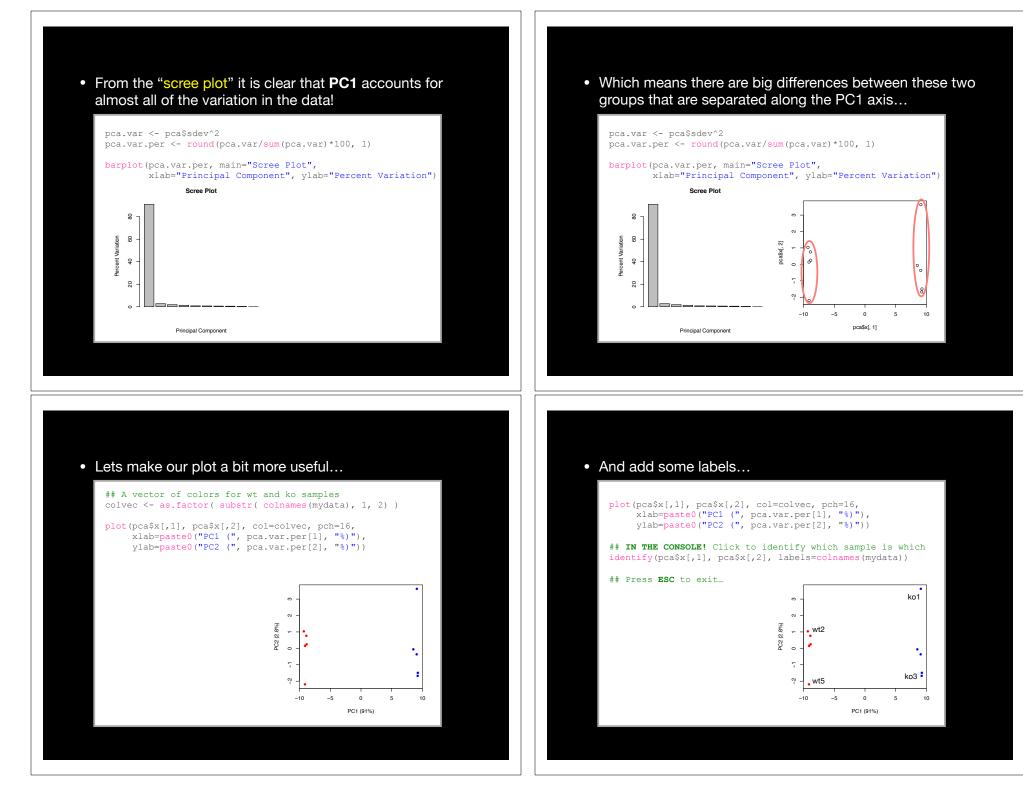
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pca.var <- pca\$sdev^2
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### Your turn!

Perform a PCA on the UK foods dataset

https://bioboot.github.io/bggn213 W20/class-material/lab-8-bggn213.html

Input: read, View/head, PCA: prcomp, Plots: PCA plot scree plot, loadings plot.

#### [Muddy Point Feedback Link]

#### Main PCA objectives include:

- To reduce dimensionality
- To visualize multidimensional data
- To choose the most useful variables (features)
- To identify groupings of objects (e.g. genes/samples)
- To identify outliers

## **Reference Slides**

- Finally, lets look at how to use the loading scores to determine which genes have the largest effect on where samples are plotted in the PCA plot
  - The prcomp() function calls loading scores \$rotation

## Lets focus on PC1 as it accounts for > 90% of variance loading\_scores <- pca\$rotation[,1]</pre>

- Finally, lets look at how to use the loading scores to determine which genes have the largest effect on where samples are plotted in the PCA plot
  - The prcomp() function calls loading scores \$rotation

## Lets focus on PC1 as it accounts for > 90% of variance loading\_scores <- pca\$rotation[,1]</pre>

summary(loading\_scores) Min. 1st Qu. Median Mean 3rd Qu. Max. -0.104763 -0.104276 -0.068784 -0.005656 0.103926 0.104797

## We are interested in the magnitudes of both plus
## and minus contributing genes
gene scores <- abs(loading scores)</pre>

- Finally, lets look at how to use the loading scores to determine which genes have the largest effect on where samples are plotted in the PCA plot
  - The prcomp() function calls loading scores \$rotation

loading scores <- pca\$rotation[,1]</pre>

gene scores <- abs(loading scores)

## Sort by magnitudes from high to low
gene score ranked <- sort(gene scores, decreasing=TRUE)</pre>

## Find the names of the top 5 genes
top\_5\_genes <- names(gene\_score\_ranked[1:5])</pre>

- Finally, lets look at how to use the loading scores to determine which genes have the largest effect on where samples are plotted in the PCA plot
  - The prcomp() function calls loading scores \$rotation

loading\_scores <- pca\$rotation[,1]</pre>

gene\_scores <- abs(loading\_scores)</pre>

## Sort by magnitudes from high to low
gene\_score\_ranked <- sort(gene\_scores, decreasing=TRUE)</pre>

- Finally, lets look at how to use the loading scores to determine which genes have the largest effect on where samples are plotted in the PCA plot
  - The prcomp() function calls loading scores \$rotation

loading scores <- pca\$rotation[,1]</pre>

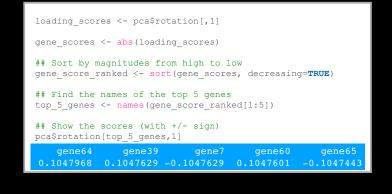
gene\_scores <- abs(loading\_scores)

## Sort by magnitudes from high to low
gene\_score\_ranked <- sort(gene\_scores, decreasing=TRUE)</pre>

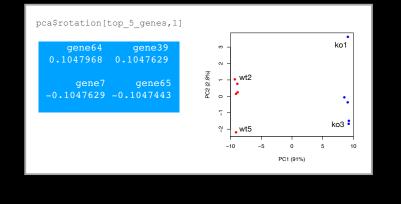
## Find the names of the top 5 genes
top\_5\_genes <- names(gene\_score\_ranked[1:5])</pre>

## Show the scores (with +/- sign)
pca\$rotation[top\_5\_genes,1]

- Here we see genes with the largest positive loading scores that effectively 'push' the "ko" samples to the right positive side of the plot.
- And the genes with high negative scores that push "wt" samples to the left side of the plot.



- Here we see genes with the largest positive loading scores that effectively 'push' the "ko" samples to the right positive side of the plot.
- And the genes with high negative scores that push "wt" samples to the left side of the plot.



### **PCA Summary**

- PCA is classic "multivariate statistical technique" used to reduce the dimensionality of a complex data set to a more manageable number (typically 2D or 3D)
- For a matrix of *m* genes x *n* samples, we mean center (i.e. subtract the sample mean from each sample column), optionally rescale the values for each sample column, then calculate a new covariance matrix of size *n* x *n*
- We finally diagonalize the covariance matrix to yield our *n* Eigenvectors (called principal components or PCs) and *n* Eigenvalues.
- The top PCs (with largest Eigenvalues) retain the essential features of the original data and represent a useful subspace for further analysis (e.g. visualization, clustering, feature extraction, outlier detection etc...)

# Practical issues with PCA

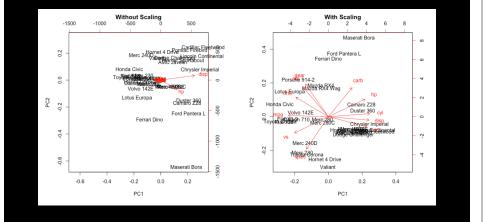
- Scaling the data
- Missing values:

### Scaling

<pre>&gt; data(mtcars)</pre>												
head(mtcars)												
	mpg	cyl	disp	hp	drat	wt	qsec	vs	am	gear	carb	
Mazda RX4	21.0	6	160	110	3.90	2.620	16.46	0	1	4	4	
Mazda RX4 Wag	21.0	6	160	110	3.90	2.875	17.02	0	1	4	4	
Datsun 710	22.8	4	108	93	3.85	2.320	18.61	1	1		1	
Hornet 4 Drive	21.4	6	258	110	3.08	3.215	19.44	1	0	-	1	
Hornet Sportabout	18.7	8	360	175	3.15	3.440	17.02	-	-	3	2	
Valiant	18.1	6	225	105	2.76	3.460	20.22	1	0	3	1	
# Means and standa	ard de	eviat	tions	vary	/ a lo	ot						
> round(colMeans(r	ntcars	5), 2	2)									
mpg cyl d <sup>-</sup>	isp	h	o dr	at	wt	t qse	ec	vs		am	gear	carb
20.09 6.19 230	.72 14	16.69	ЭЗ.	.60	3.22	2 17.8	35 0	.44	6	9.41	3.69	2.81
> round(apply(mtca	ars, 2	2, so	1), 2)	)								
mpg cyl d <sup>-</sup>	isp	h	o dr	at	wt	t qse	ec	vs		am	gear	carb
6.03 1.79 123	.94 6	58.50	50.	53	0.98	3 1.7	79 0	.50	6	9.50	0.74	1.62

### Scaling

prcomp(x, center=TRUE, scale=FALSE)
prcomp(x, center=TRUE, scale=TRUE)



### Practical issues with PCA

- Scaling the data
- Missing values:
  - Drop observations with missing values
  - Impute / estimate missing values