

Recap of Lecture 7

- Reviewed the major steps for R function writing
- Introduced the CRAN & Bioconductor repositories for packages that extend R functionality
- Explored installing and using the ggplot2, bio3d, rgl, rentrez, igraph, blogdown, shiny, and other packages
- Discussed how to judge the utility, usability and development status of R packages.

[Muddy Point Feedback Link]

Today's Menu

- Introduction to machine learning
 - <u>Unsupervised</u>, supervised and reinforcement learning
- Clustering
 - K-means clustering
 - Hierarchical clustering
 - Heatmap representations
- Dimensionality reduction, visualization and 'structure' analysis
 - Principal Component Analysis (PCA)
- Hands-on application to cell classification

Types of machine learning

- <u>Unsupervised learning</u>
 - Finding structure in unlabeled data
- Supervised learning
 - Making predictions based on labeled data
 - Predictions like regression or classification
- <u>Reinforcement learning</u>
 - Making decisions based on past experience

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- Breaks observations into *k* pre-defined number of clusters
- You define *k* the number of clusters!

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Here your eyes can clearly see 3 natural groupings

k-means clustering algorithm

- Breaks observations into *k* pre-defined number of clusters
- You define *k* the number of clusters!
 - Imagine you had data that you could plot along a line and you knew you had to put them into k=3 "clusters" (e.g. data from three types of tumor cells)



Here your eyes can clearly see 3 natural groupings How does k-means attempt to define this grouping?

Step 1. Select *k* (the number of clusters)

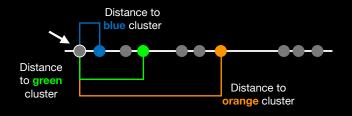


Step 2. Select *k=3* distant data points at random These are the initial clusters



Step 3.

Measure distance between the 1st point and the *k=3* initial clusters



Step 4. Assign the 1st point to the nearest cluster



Step 5.

Update cluster centers

Calculate the mean value for the blue cluster including the new point

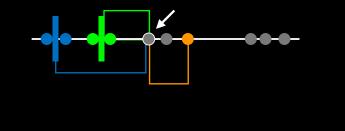


Step 6.

Assign next point to closest cluster Use updated cluster centers for distance calculation

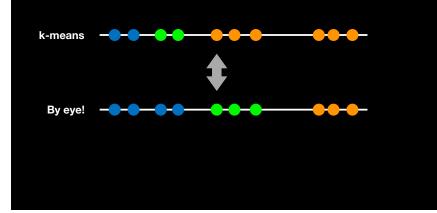


Step 7. Update cluster centers and move to next point Use updated cluster centers for distance calculation

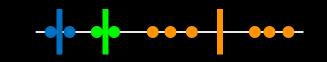


Hmm....

Here the k-means result does not look as good as what we were able to do by eye!

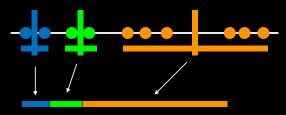


Step 8. Repeat for each point Each time updating cluster centers



Step 9.

Assess the quality of the clustering by adding up the variation within each cluster

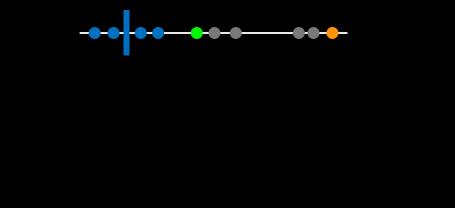


The total variation within clusters

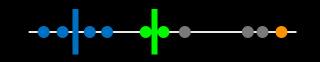
K-means keeps track of these clusters and their total **variance** and then does the whole thing over again with different starting points

...Pick k=3 initial clusters and add the remaining points to Step 10. the cluster with the nearest mean, recalculating the mean Repeat with different starting points each time a new point is added... Back to the beginning and do all steps over again... Pick new points as "initial" clusters ...Pick k=3 initial clusters and add the remaining points to ...Pick k=3 initial clusters and add the remaining points to the cluster with the nearest mean, recalculating the mean the cluster with the nearest mean, recalculating the mean each time a new point is added... each time a new point is added...

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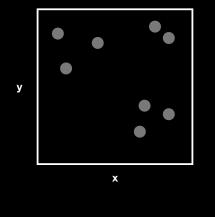


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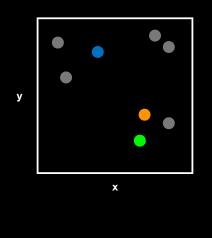


Now the data are all assigned to clusters, we again sum ...Pick k=3 initial clusters and add the remaining points to the cluster with the nearest mean, recalculating the mean the variation within each cluster each time a new point is added... The total variation within clusters After several iterations k-means clustering knows it has the Step 10. best clustering so-far based on the smallest total variation Repeat again with different starting points with clusters. However, it does not know if it has found the *best overall*. So it will perform several more iterations with different starting points... Iteration 1 Iteration 2 The winner! **Iteration 3** Iteration 4 The total variation within clusters

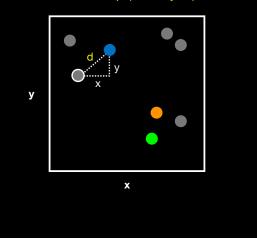
What if we have more dimensions?



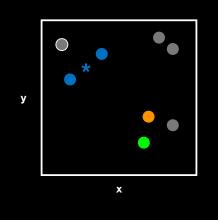
Just like before, we pick 3 random points...

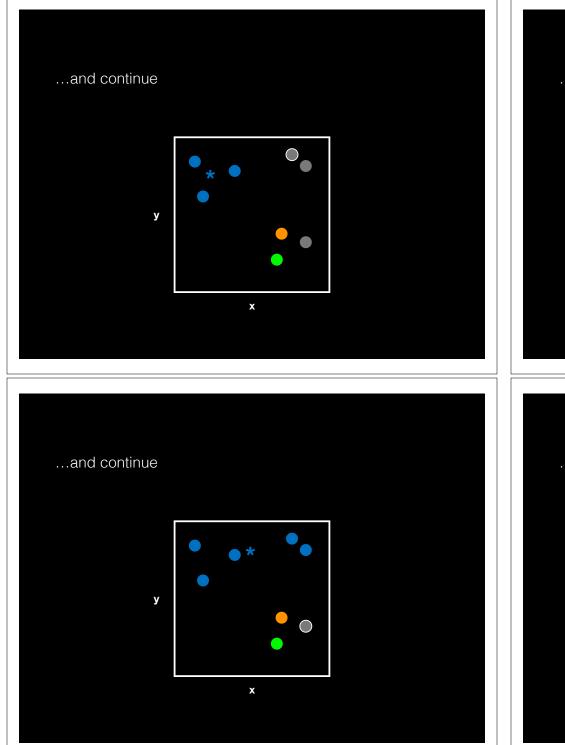


...and use the Euclidean distance. In 2 dimensions the Euclidean distance is the same as the Pythagorean theorem $d = sqrt(x^2 + y^2)$

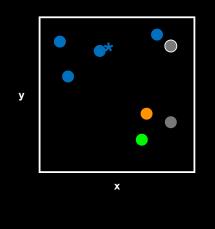


...assign point to nearest cluster and update cluster center \star

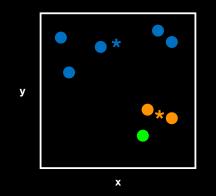




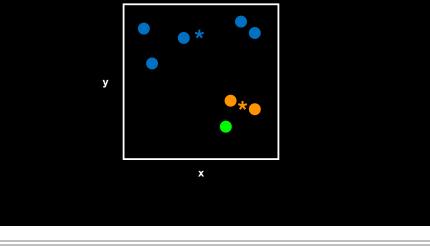
...and continue



...and continue



Again we have to use a number of different starting conditions before deciding on a good clustering!



What if we have even more dimensions?

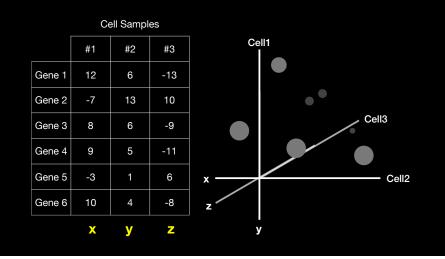
	Cell Samples				
	#1	#2	#3		
Gene 1	12	6	-13		
Gene 2	-7	13	10		
Gene 3	8	6	-9		
Gene 4	9	5	-11		
Gene 5	-3	1	6		
Gene 6	10	4	-8		

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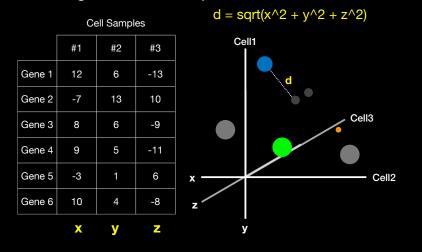
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	X	У	z	

We could simply plot them by relabeling the cell samples as **x**, **y**, and **z** (i.e. a 3D plot)

What if we have even more dimensions?



...and go through exactly the same procedure with initial cluster assignment followed by distance calculation etc...



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 $d = sqrt(x^2 + y^2 + z^2)$

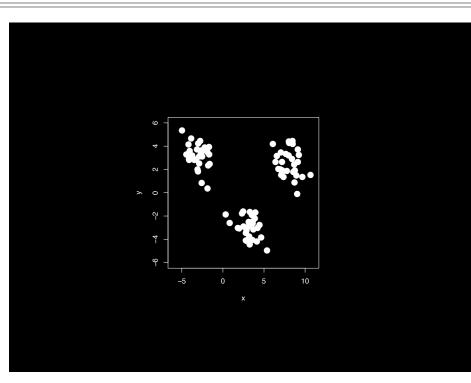
Of course we don't actually need to plot anything.

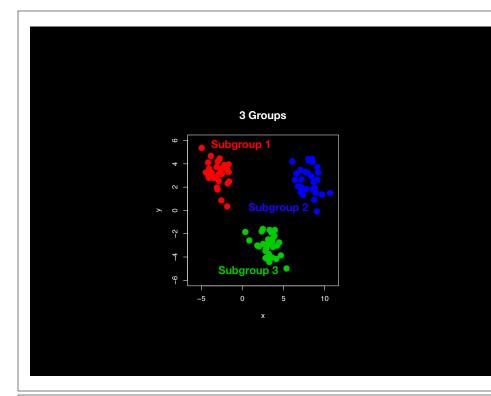
We can just calculate the Euclidean distance along any number of dimensions and perform our k-means clustering in the same way.

k-means in R

k-means algorithm with 3 centers, run 20 time
kmeans(x, centers= 3, nstart= 20)

- Input x is a numeric matrix, or data.frame, with one observation per row, one feature per column
- k-means has a random component
- Run algorithm multiple times to improve odds of the best model





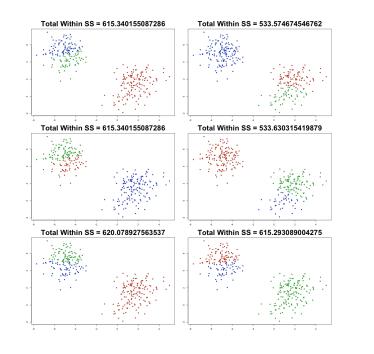
Model selection

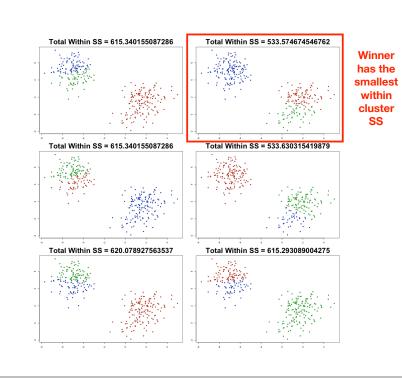
- · Recall k-means has a random component
- Best outcome is based on total within cluster sum of squares:
 - For each cluster
 - For each observation in the cluster
 - Determine squared distance from observation to cluster center
 - Sum all of them together

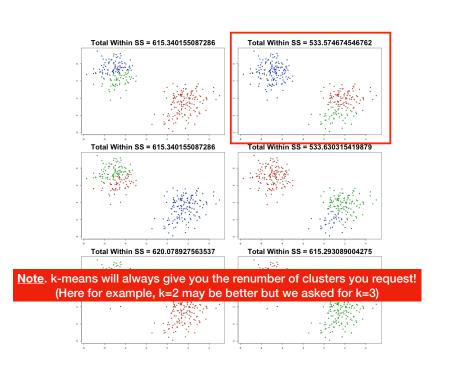
Model selection

k-means algorithm with 5 centers, run 20 times
kmeans(x, centers=5, nstart=20)

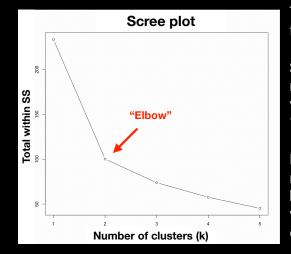
- Running algorithm multiple times (i.e. setting nstart) helps find the global minimum total within cluster sum of squares
- Increasing the default value of **nstart** is often sensible







Determining number of clusters



Trial and error is not the best approach

Systematically try a range of different k values and plot a "scree plot".

Here there is a large reduction in SS with **k=2** but after that the values do not go down as quickly!

Your Turn!

Generate some example data for clustering
tmp <- c(rnorm(30,-3), rnorm(30,3))
x <- cbind(x=tmp, y=rev(tmp))</pre>

plot(x)

Use the kmeans() function setting k to 2 and nstart=20

Inspect/print the results

- Q. How many points are in each cluster?
- Q. What 'component' of your result object details - cluster size?
 - cluster size?
 - cluster assignment/membership?
 - cluster center?

Plot x colored by the kmeans cluster assignment and add cluster centers as blue points

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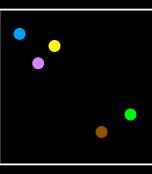
Hierarchical clustering

- Number of clusters is not known ahead of time
- Two kinds of hierarchical clustering:
 - bottom-up
 - top-down

Hierarchical clustering

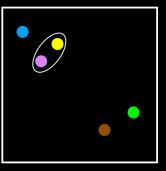
Simple example:

5 clusters: Each point starts as it's own "cluster"!



Hierarchical clustering

4 clusters



Hierarchical clustering Hierarchical clustering 3 clusters 2 clusters Hierarchical clustering Hierarchical clustering in R End: 1 cluster dist matrix <- dist(x)</pre>

Lets have a closer look...

Our input is a distance matrix from the dist()
function. Lets make sure we understand it first
dist_matrix <- dist(x)</pre>

dim(dist_matrix)
NULL

View(as.matrix(dist_matrix))

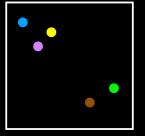
dim(x)
[1] 60 2

dim(as.matrix(dist_matrix)
[1] 60 60

Note. symmetrical pairwise distance matrix

Dendrogram

• Tree shaped structure used to interpret hierarchical clustering models



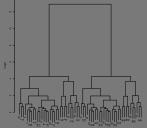


Interpreting results

Create hierarchieal cluster model: he
hc <- hclust(dist(x))</pre>

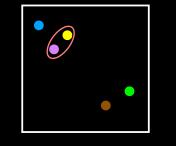
We can plot the results as a dendrogram
plot(hc)

What do you notice?
Does the dendrogram
make sense based on
your knowledge of x?

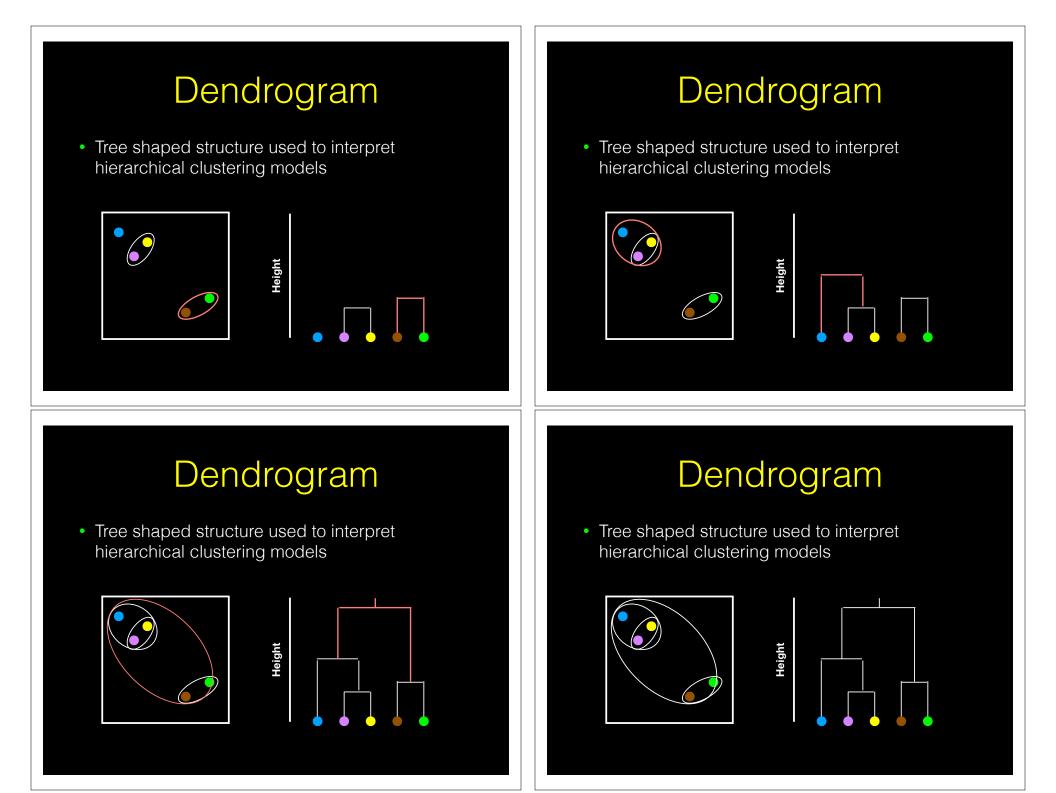


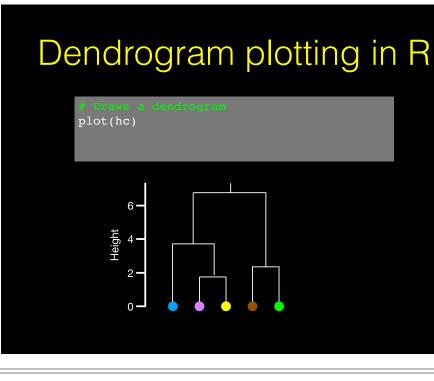
Dendrogram

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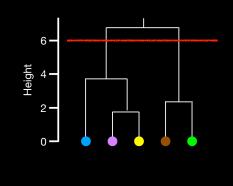






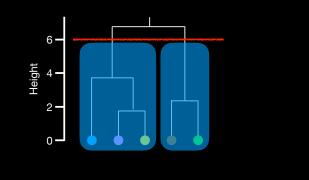
Dendrogram plotting in R

Draws a dendrogram
plot(hc)
abline(h=6, col="red")

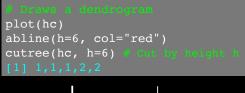


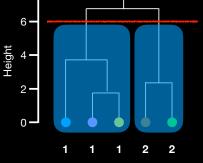
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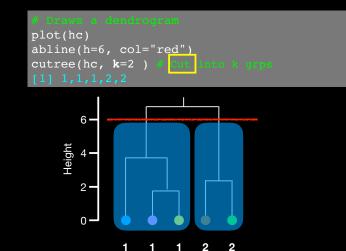


Dendrogram plotting in R





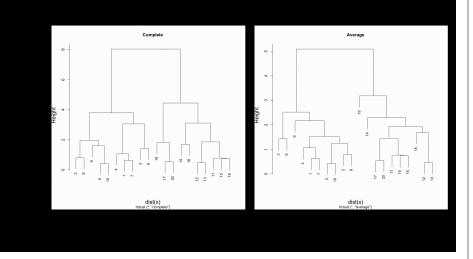
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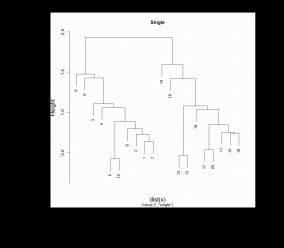
Linking clusters in hierarchical clustering

- How is distance between clusters determined?
- There are four main methods to determine which cluster should be linked:
 - Complete: pairwise similarity between all observations in cluster 1 and cluster 2, and uses largest of similarities
 - Single: same as above but uses smallest of similarities
 - Average: same as above but uses average of similarities
 - Centroid: finds centroid of cluster 1 and centroid of cluster 2, and uses similarity between two centroids

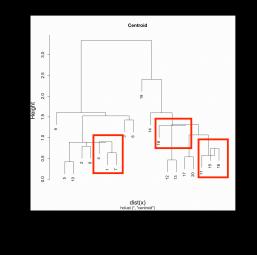
Linking methods: complete and average



Linking method: single



Linking method: centroid



Linkage in R

Using different hierarchical clustering methods
hc.complete <- hclust(d, method="complete")</pre>

hc.average <- hclust(d, method="average")</pre>

hc.single <- hclust(d, method="single")</pre>

Your Turn!

Step 1. Generate some example data for clustering
x <- rbind(</pre>

colnames(x) <- c("x", "y")</pre>

Step 2. Plot the data without clustering
plot(x)

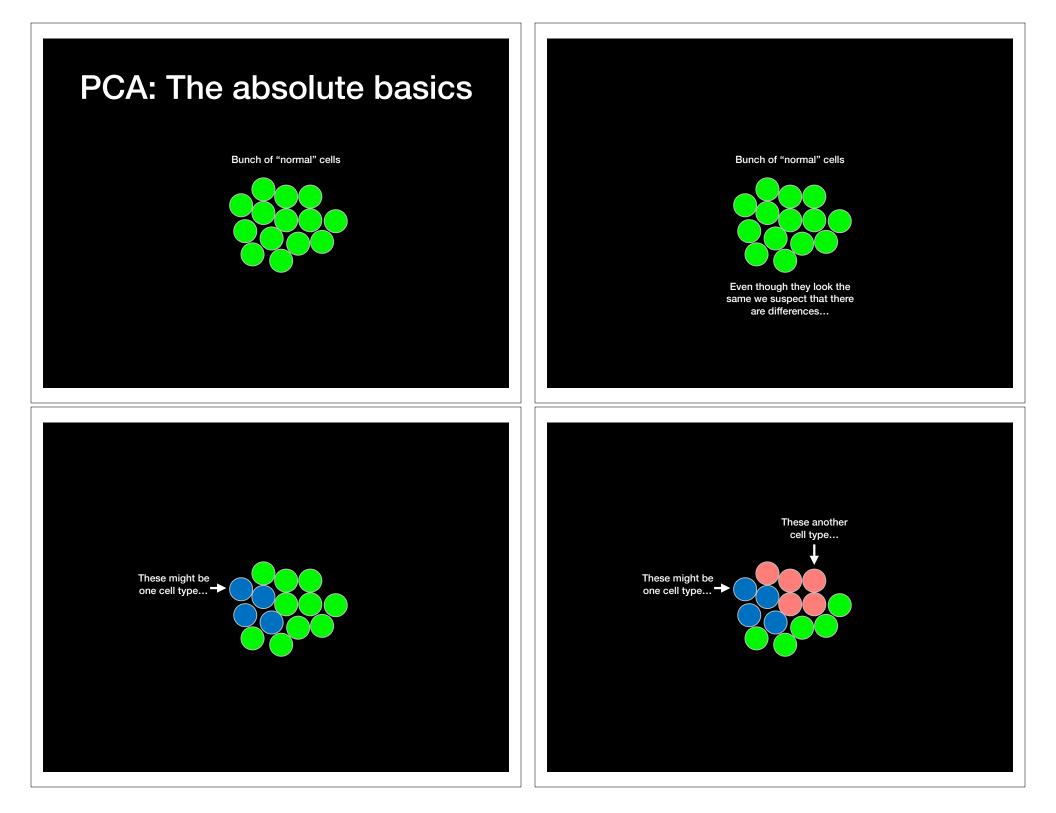
Step 3. Generate colors for known clusters
(just so we can compare to holust results)
col <- as.factor(rep(c("c1","c2","c3"), each=50))</pre>

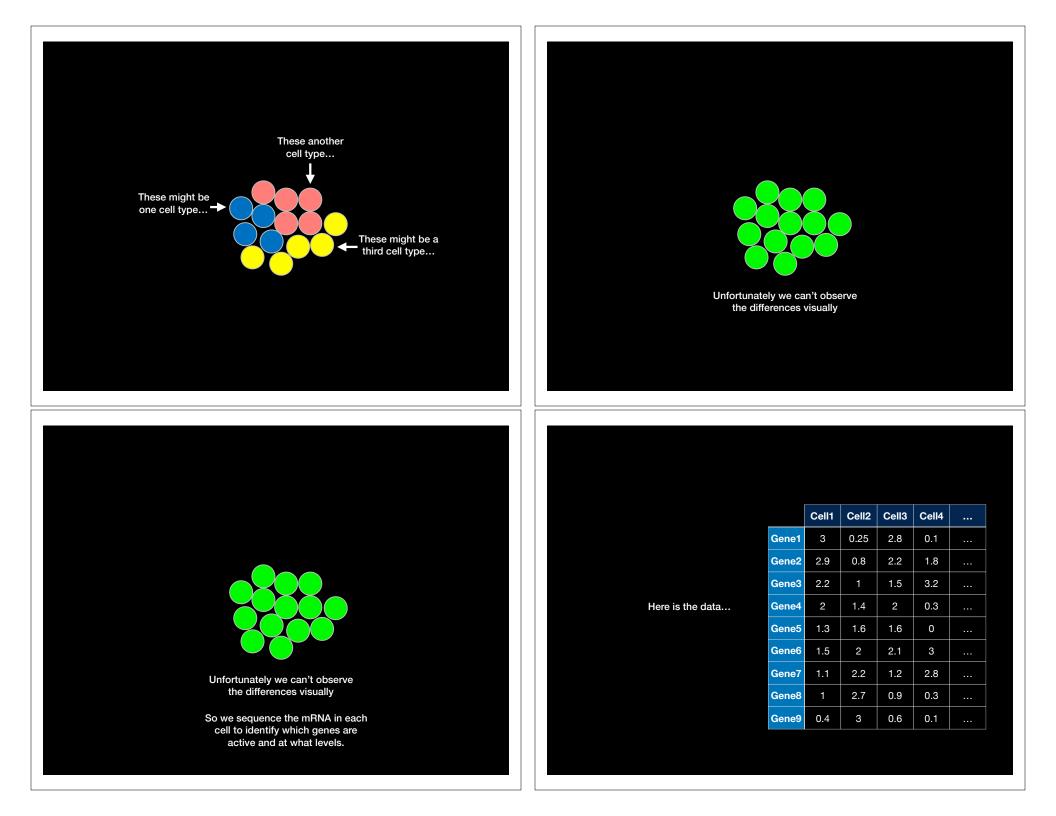
plot(x, col=col)

- Q. Use the dist(), hclust(), plot() and cutree()
 functions to return 2 and 3 clusters
- Q. How does this compare to your known 'col' groups?

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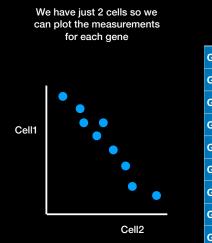


Each column shows how much each gene is transcribed in each cell

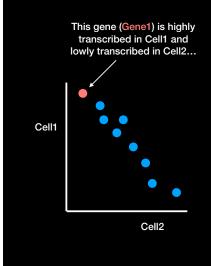
	Cell1	Cell2	Cell3	Cell4	
Gene1	3	0.25	2.8	0.1	
Gene2	2.9	0.8	2.2	1.8	
Gene3	2.2	1	1.5	3.2	
Gene4	2	1.4	2	0.3	
Gene5	1.3	1.6	1.6	0	
Gene6	1.5	2	2.1	3	
Gene7	1.1	2.2	1.2	2.8	
Gene8	1	2.7	0.9	0.3	
Gene9	0.4	3	0.6	0.1	

Here is the data...

	Cell1	Cell2
Gene1	3	0.25
Gene2	2.9	0.8
Gene3	2.2	1
Gene4	2	1.4
Gene5	1.3	1.6
Gene6	1.5	2
Gene7	1.1	2.2
Gene8	1	2.7
Gene9	0.4	3

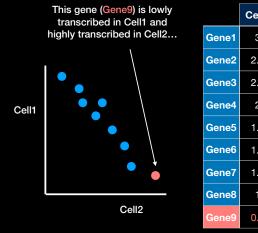


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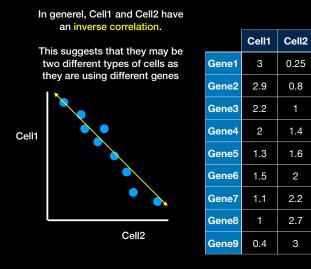


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For now lets consider only two cells



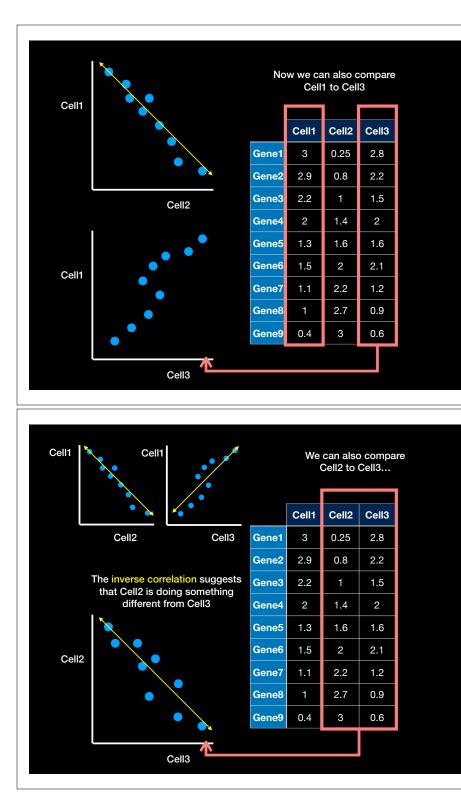
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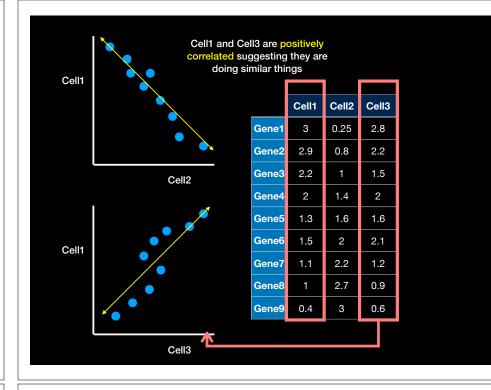


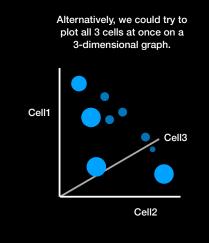
Cell1		We have alre plot the first closely		lls to see	e how	
			0.114	0.110	0	
			Cell1	Cell2	Cell3	
		Gene1	3	0.25	2.8	
		Gene2	2.9	0.8	2.2	
	Cell2	Gene3	2.2	1	1.5	
		Gene4	2	1.4	2	
		Gene5	1.3	1.6	1.6	
		Gene6	1.5	2	2.1	
		Gene7	1.1	2.2	1.2	
		Gene8	1	2.7	0.9	
		Gene9	0.4	3	0.6	

		Cell1	Cell2	Cell3
	Gene1	3	0.25	2.8
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	Gene3	2.2	1	1.5
ow lets imagine are are three cells	Gene4	2	1.4	2
	Gene5	1.3	1.6	1.6
	Gene6	1.5	2	2.1
	Gene7	1.1	2.2	1.2
	Gene8	1	2.7	0.9
	Gene9	0.4	3	0.6

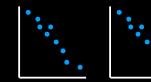
Ν the

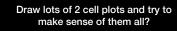






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Gene6	1.5	2	2.1	3	
Gene7	1.1	2.2	1.2	2.8	
Gene8	1	2.7	0.9	0.3	
Gene9	0.4	3	0.6	0.1	

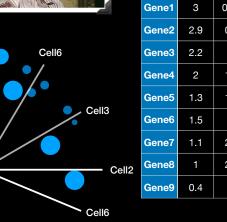
But what if we have 4 or more Cells?

	Cell1	Cell2	Cell3	Cell4	
Gene1	3	0.25	2.8	0.1	
Gene2	2.9	0.8	2.2	1.8	
Gene3	2.2	1	1.5	3.2	
Gene4	2	1.4	2	0.3	
Gene5	1.3	1.6	1.6	0	
Gene6	1.5	2	2.1	3	
Gene7	1.1	2.2	1.2	2.8	
Gene8	1	2.7	0.9	0.3	
Gene9	0.4	3	0.6	0.1	

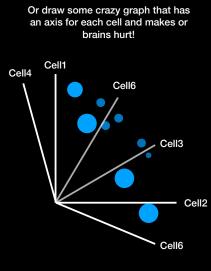


Cell1

Cell4

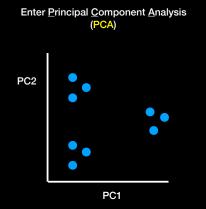


	Cell1	Cell2	Cell3	Cell4	
Gene1	3	0.25	2.8	0.1	
Gene2	2.9	0.8	2.2	1.8	
Gene3	2.2	1	1.5	3.2	
Gene4	2	1.4	2	0.3	
Gene5	1.3	1.6	1.6	0	
Gene6	1.5	2	2.1	3	
Gene7	1.1	2.2	1.2	2.8	
Gene8	1	2.7	0.9	0.3	
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	Cell1	Cell2	Cell3	Cell4	
Gene1	ne1 3 0.25		2.8	0.1	
Gene2	2.9	0.8	2.2	1.8	
Gene3	2.2	1	1.5	3.2	
Gene4	2	1.4	2	0.3	
Gene5	1.3	1.6	1.6	0	
Gene6	1.5	2	2.1	3	
Gene7	1.1	2.2	1.2	2.8	
Gene8	1	2.7	0.9	0.3	
Gene9	0.4	3	0.6	0.1	

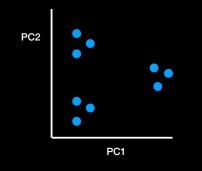
0 110



PC1

	Cell1	Cell2	Cell3	Cell4	
Gene1	3	0.25	2.8	0.1	
Gene2	2.9	0.8	2.2	1.8	
Gene3	2.2	1	1.5	3.2	
Gene4	2	1.4	2	0.3	
Gene5	1.3	1.6	1.6	0	
Gene6	1.5	2	2.1	3	
Gene7	1.1	2.2	1.2	2.8	
Gene8	1	2.7	0.9	0.3	
Gene9	0.4	3	0.6	0.1	

PCA converts the correlations (or lack there of) among all cells into a representation we can more readily interpret (e.g. a 2D graph!)

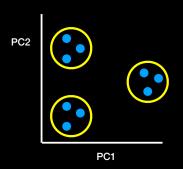


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Gene8	1	2.7	0.9	0.3	
Gene9	0.4	3	0.6	0.1	

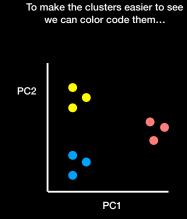
Cells that are highly correlated			Cell1	Cell2	Cell3	Cell4
	cluster together	Gene1	3	0.25	2.8	0.1
		Gene2	2.9	0.8	2.2	1.8
		Gene3	2.2	1	1.5	3.2
PC2		Gene4	2	1.4	2	0.3
		Gene5	1.3	1.6	1.6	0
	•	Gene6	1.5	2	2.1	3
		Gene7	1.1	2.2	1.2	2.8
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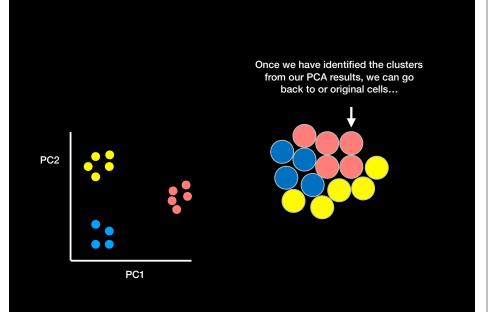
Cells that are highly correlated cluster together

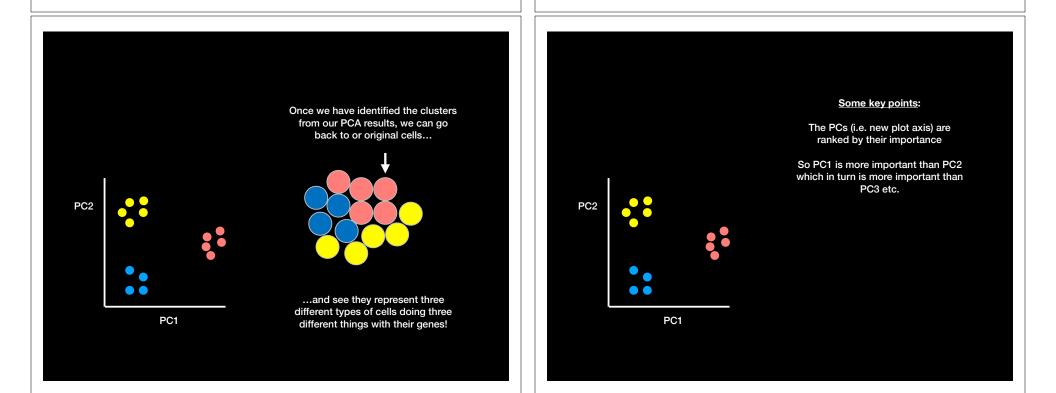


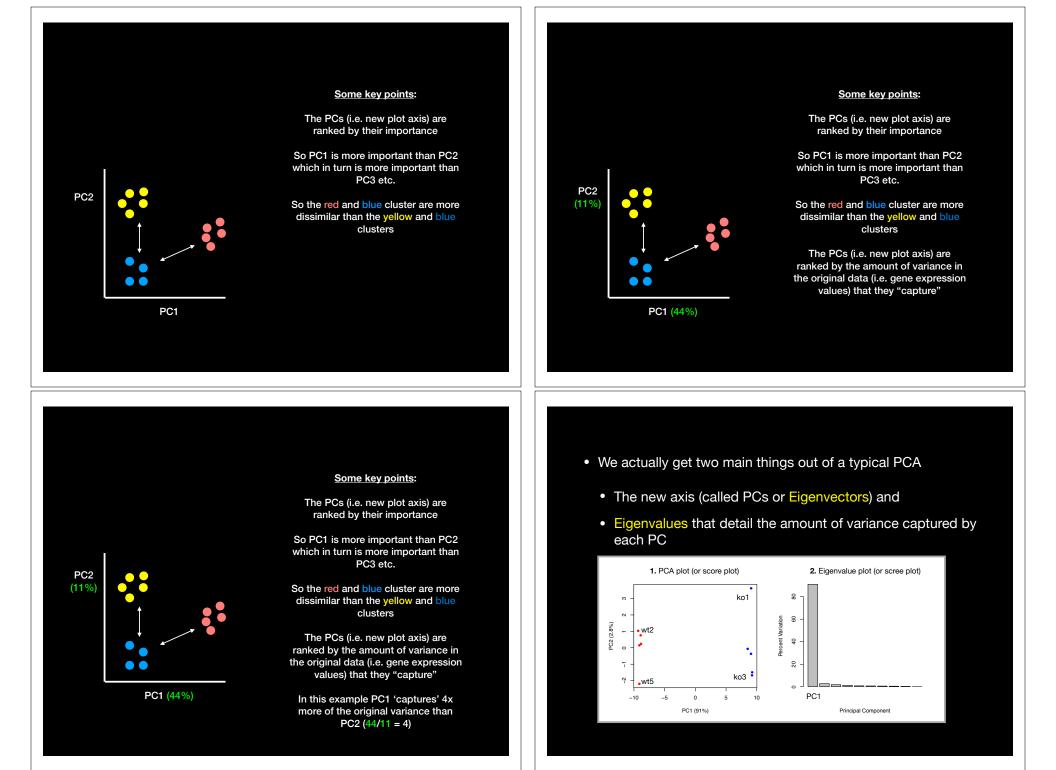
	Cell1	Cell2	Cell3	Cell4	
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Gene5	1.3	1.6	1.6	0	
Gene6	1.5	2	2.1	3	
Gene7	1.1	1 2.2 1.2 2.8		2.8	
Gene8	1	2.7 0.9 0.5		0.3	
Gene9	0.4	3	0.6	0.1	







- Another cool thing we can get out of PCA is a quantitive report on how the original variables contributed to each PC
 - In other words, which were the most important genes that lead to the observed clustering in PC-space
 - These are often called the loadings and we can plot them to see which are the most important genes for the observed separation as well as outputting ranked lists of genes that act to discriminate the samples



Hands-on time!

https://bioboot.github.io/bimm143_W19/class-material/pca/

Outline: How to do PCA in R

- How to use the **prcomp()** function to do PCA.
- How to draw and interpret PCA plots
- How to determine how much variation each principal component accounts for and the the "intrinsic dimensionality" useful for further analysis
- How to examine the **loadings** (or loading scores) to determine what variables have the largest effect on the graph and are thus important for discriminating samples.

• First lets read our example data to work with.

head(mydata)

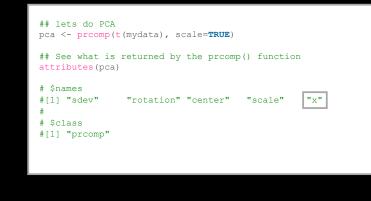
	wt1	wt2	wt3	wt4	wt5	ko1	ko2	ko3	ko4	ko5
gene1	147	171	160	175	187	63	57	58	55	59
gene2	151	134	148	126	134	838	831	894	847	830
gene3	702	672	653	681	701	593	579	644	596	610
gene4	319	297	310	296	304	754	807	734	750	774
gene5	168	147	162	142	152	787	811	814	869	784

• NOTE: the samples are columns, and the genes are rows!

- Now we have our data we call **prcomp()** to do PCA
 - NOTE: prcomp() expects the samples to be rows and genes to be columns so we need to first transpose the matrix with the t() function!

lets do PCA
pca <- prcomp(t(mydata), scale=TRUE)</pre>

- The returned pca\$x here contains the principal components (PCs) for drawing our first graph.
 - Here we will take the first two columns in pca\$x (corresponding to PC1 and PC2) to draw a 2-D plot



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lets do PCA
pca <- prcomp(t(mydata), scale=TRUE)</pre>

See what is returned by the prcomp() function
attributes(pca)

\$names
#[1] "sdev" "rotation" "center" "scale" "x"
#

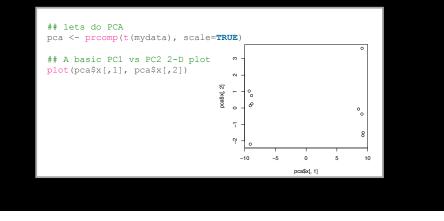
\$class #[1] "prcomp"

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A basic PC1 vs PC2 2-D plot
plot(pca\$x[,1], pca\$x[,2])

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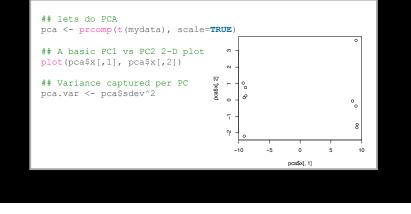
- Looks interesting with a nice separation of samples into two groups of 5 samples each
 - Now we can use the square of pca\$sdev, which stands for "standard deviation", to calculate how much variation in the original data each PC accounts for

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pca.var.per

[1] 91.0 2.8 1.9 1.3 0.8 0.7 0.6 0.5 0.3 0.0

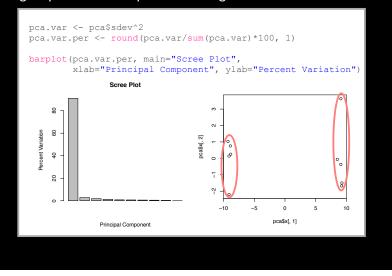
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```
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```

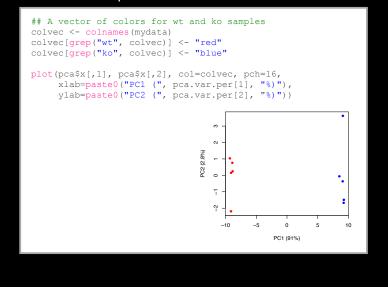
 • From the "scree plot" it is clear that **PC1** accounts for almost all of the variation in the data!

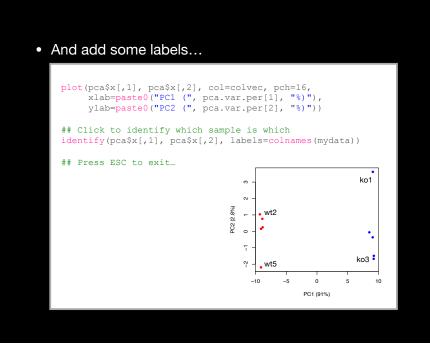


• Which means there are big differences between these two groups that are separated along the PC1 axis...



• Lets make our plot a bit more useful...





Your turn!

Perform a PCA on the UK foods dataset

https://bioboot.github.io/bimm143 W19/class-material/lab-8-bimm143.html

Input: read, View/head, PCA: prcomp, Plots: PCA plot scree plot, loadings plot.

[Muddy Point Feedback Link]

Main PCA objectives include:

- To reduce dimensionality
- To visualize multidimensional data
- To choose the most useful variables (features)
- To identify groupings of objects (e.g. genes/samples)
- To identify outliers

Reference Slides

- Finally, lets look at how to use the loading scores to determine which genes have the largest effect on where samples are plotted in the PCA plot
 - The prcomp() function calls loading scores \$rotation

Lets focus on PC1 as it accounts for > 90% of variance loading scores <- pca\$rotation[,1]</pre>

- Finally, lets look at how to use the loading scores to determine which genes have the largest effect on where samples are plotted in the PCA plot
 - The prcomp() function calls loading scores \$rotation

loading scores <- pca\$rotation[,1]</pre>

gene scores <- abs(loading scores)</pre>

Sort by magnitudes from high to low
gene score ranked <- sort(gene scores, decreasing=TRUE)</pre>

- Finally, lets look at how to use the loading scores to determine which genes have the largest effect on where samples are plotted in the PCA plot
 - The prcomp() function calls loading scores \$rotation

Lets focus on PC1 as it accounts for > 90% of variance loading_scores <- pca\$rotation[,1]</pre>

summary(loading_scores) Min. 1st Qu. Median Mean 3rd Qu. Max. -0.104763 -0.104276 -0.068784 -0.005656 0.103926 0.104797

We are interested in the magnitudes of both plus
and minus contributing genes
gene scores <- abs(loading scores)</pre>

- Finally, lets look at how to use the loading scores to determine which genes have the largest effect on where samples are plotted in the PCA plot
 - The prcomp() function calls loading scores \$rotation

loading scores <- pca\$rotation[,1]</pre>

gene_scores <- abs(loading_scores)

Sort by magnitudes from high to low
gene_score_ranked <- sort(gene_scores, decreasing=TRUE)</pre>

Find the names of the top 5 genes
top_5_genes <- names(gene_score_ranked[1:5])</pre>

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Show the scores (with +/- sign)
pca\$rotation[top_5_genes,1]

- Here we see genes with the largest positive loading scores that effectively 'push' the "ko" samples to the right positive side of the plot.
- And the genes with high negative scores that push "wt" samples to the left side of the plot.

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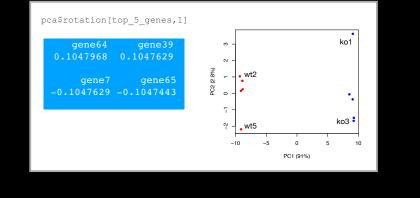
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pca\$rotation[top_5_genes,1]

gene64 gene39 gene7 gene60 gene65 .1047968 0.1047629 -0.1047629 0.1047601 -0.1047443

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PCA Recap

- PCA is classic "multivariate statistical technique" used to reduce the dimensionality of a complex data set to a more manageable number (typically 2D or 3D)
- For a matrix of *m* genes x *n* samples, we mean center (i.e. subtract the sample mean from each sample column), optionally rescale the values for each sample column, then calculate a new covariance matrix of size *n* x *n*
- We finally diagonalize the covariance matrix to yield our *n* Eigenvectors (called principal components or PCs) and *n* Eigenvalues.
- The top PCs (with largest Eigenvalues) retain the essential features of the original data and represent a useful subspace for further analysis (e.g. visualization, clustering, feature extraction, outlier detection etc...)

Practical issues with PCA

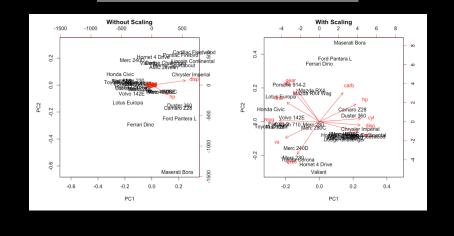
- Scaling the data
- Missing values:

Scaling

> data(mtcars) > head(mtcars) mpg cyl disp hp drat wt qsec vs am gear carb Mazda RX4 21.0 6 160 110 3.90 2.620 16.46 Θ 1 4 4 Mazda RX4 Wag 21.0 6 160 110 3.90 2.875 17.02 ø 4 108 93 3.85 2.320 18.61 Datsun 710 22.8 1 1 Δ 1 Hornet 4 Drive 21.4 6 258 110 3.08 3.215 19.44 1 0 3 1 8 360 175 3.15 3.440 17.02 0 Hornet Sportabout 18.7 0 3 2 Valiant 18.1 6 225 105 2.76 3.460 20.22 1 0 3 1 Means and standard deviations vary a lot round(colMeans(mtcars), 2) cyl disp mpg hp drat wt asec vs am gear carb 20.09 6.19 230.72 146.69 3.60 3.22 17.85 0.44 0.41 3.69 2.81 round(apply(mtcars, 2, sd), 2) cyl disp mpg hp drat wt qsec vs am gear carb 6.03 1.79 123.94 68.56 0.53 0.98 1.79 0.50 0.50 0.74 1.62

Scaling

prcomp(x, center=TRUE, scale=FALSE)
prcomp(x, center=TRUE, scale=TRUE)



Practical issues with PCA

- Scaling the data
- Missing values:
 - Drop observations with missing values
 - Impute / estimate missing values

